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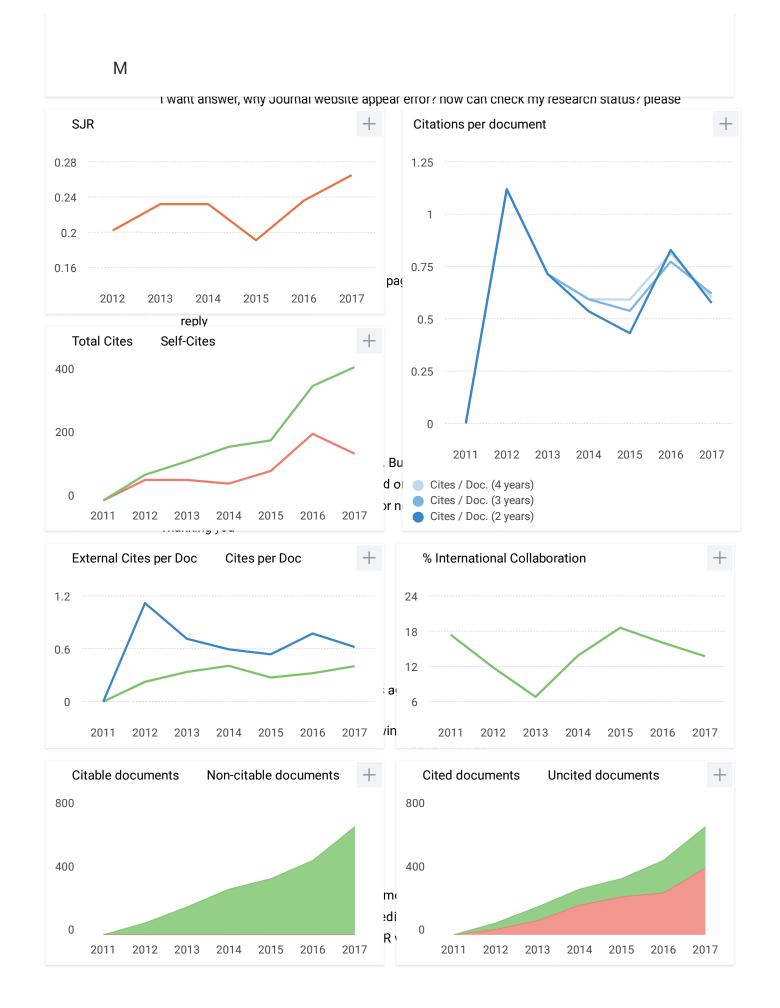
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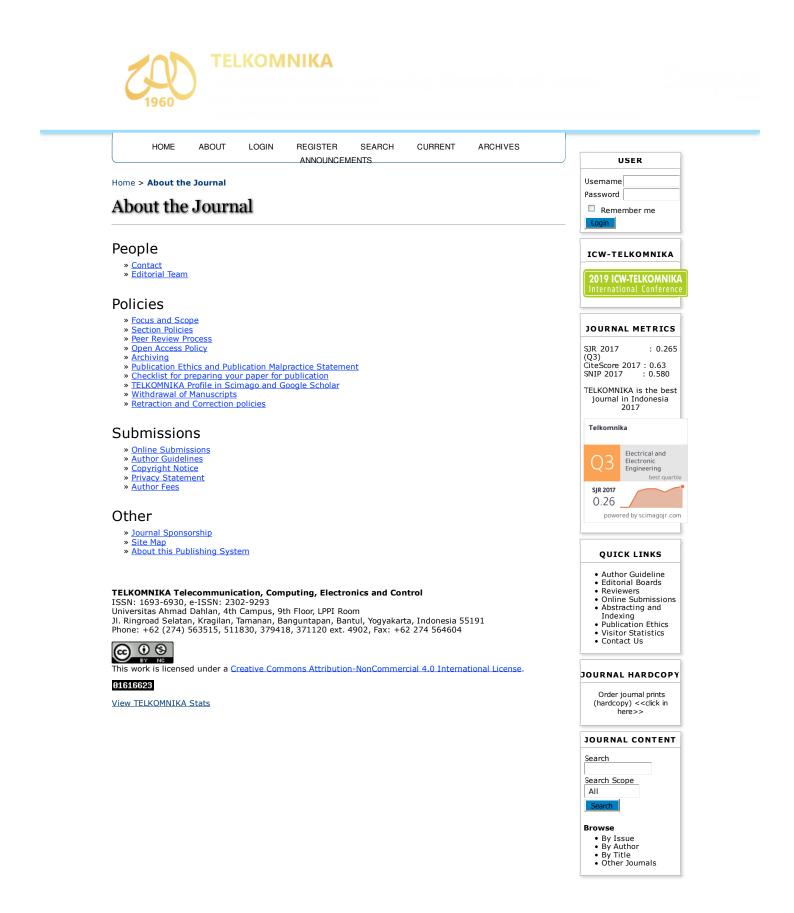
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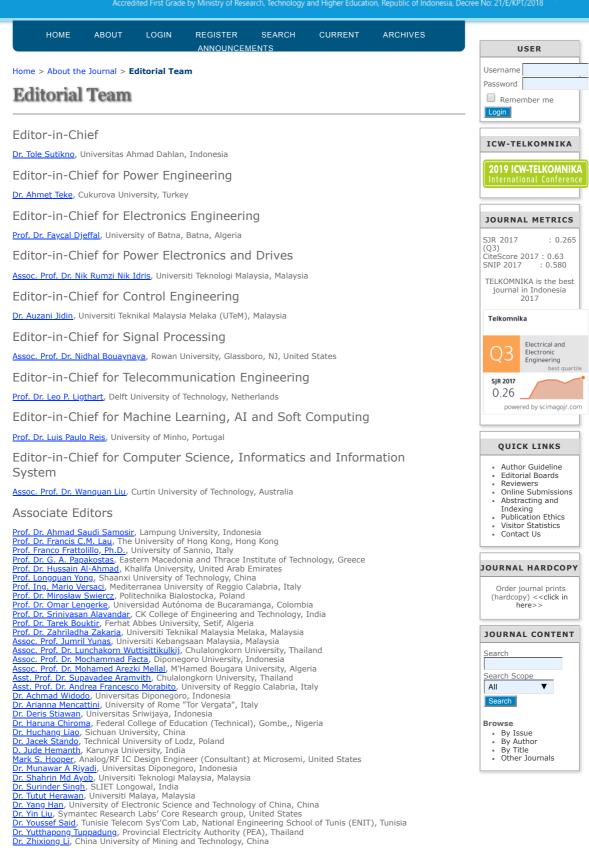


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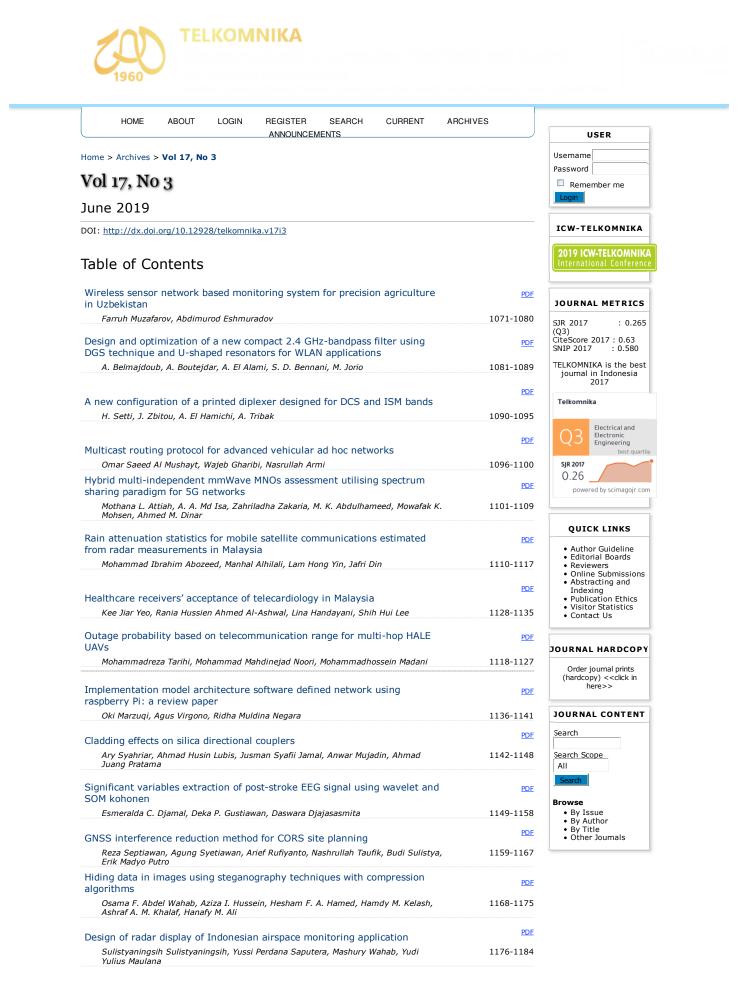


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Formal expansion method for solving an electrical circuit model

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Abstract

We investigate the validity of the formal expansion method for solving a second order ordinary differential equation raised from an electrical circuit problem. The formal expansion method approximates the exact solution using a series of solutions. An approximate formal expansion solution is a truncated version of this series. In this paper, we confirm using simulations that the approximate formal expansion solution is valid for a specific interval of domain of the free variable. The accuracy of the formal expansion approximation is guaranteed on the time-scale 1.

Keywords: damped oscillation, electrical circuit, formal expansion, van der pol equation, vibration model

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1. Introduction

Mathematics and its programming have played important roles in solving as well as designing experiments of electrical engineering problems, for example, see the work of Sutikno et al. [1-4]. To be specific, in this paper we consider electrical circuit problems. Problems in electrical circuits are often modelled into differential equations. One of the models is called the van der Pol equation. This equation is due to the Dutch physicist Balthasar van der Pol in around 1920 to describe oscillations in a triode-circuit [5]. In a specific situation with small source in oscillations, the van der Pol equation becomes a vibration model with a linear friction term. In this paper we solve the vibration model with a linear friction term, which is a modification of the van der Pol equation, using the formal expansion method.

Previous research has been conducted by a number of authors relating to the van der Pol equation [5-8] in physics [9-10], biology [11], economics [12], etc. [13-15]. Amongst them, Verhulst [5] provided a theorem about the order of accuracy of the formal expansion solution with respect to the perturbation factor in the damping term. Nevertheless, it has not been confirmed computationally when we use this method to solve the vibration model with a linear damping (friction term), especially the validity of the method relating to the interval of the free variable. Therefore, this paper shall fill this gap of research, that is, we shall validate of the formal expansion method computationally. The rest of this paper is written as follows. We provide the mathematical model and method in section 2. After that we present our research results and discussion in section 3. The paper is concluded with some remarks in section 4.

2. Mathematical Model and Method

The van der Pol equation, as the considered mathematical model, is

$$\ddot{x} + x = \mu(1 - x^2)\dot{x}$$

where μ is a positive constant [5]. When the factor $\mu(1-x^2)$ is replaced by $-\varepsilon$, where ε is a small positive constant, the model becomes

 $\ddot{x} + x = -\epsilon \dot{x}$

which is valid for x > 1 or x < -1. This model is the vibration model with a linear friction term.

The core property in the formal expansion method is given in a theorem as follows due to Verhulst [5]. We consider the initial value problem

$$\dot{\mathbf{x}} = \mathbf{f}_0(\mathbf{t}, \mathbf{x}) + \varepsilon \mathbf{f}_1(\mathbf{t}, \mathbf{x}) + \dots + \varepsilon^m \mathbf{f}_m(\mathbf{t}, \mathbf{x}) + \varepsilon^{m+1} \mathbf{R}(\mathbf{t}, \mathbf{x}, \varepsilon)$$

where $x(t_0) = \eta$ and $|t - t_0| \le h$, $x \in D \subset \mathbb{R}^n$, $0 \le \varepsilon \le \varepsilon_0$. Here η is a constant, h is a positive constant, D is a domain in the n dimension, and ε_0 is a positive constant. We assume that in this domain all functions involved in the problem are infinitely many differentiable. Then the formal expansion

$$x_0(t) + \varepsilon x_1(t) + \dots + \varepsilon^m x_m(t)$$

with $x_0(t_0) = \eta$, $x_i(t) = 0, i = 1, ..., m$ approximates the exact solution x(t) with the property

$$\left\| \mathbf{x}(t) - \left(\mathbf{x}_0(t) + \varepsilon \mathbf{x}_1(t) + \dots + \varepsilon^m \mathbf{x}_m(t) \right) \right\| = \mathbf{0}(\varepsilon^{m+1})$$

on the time-scale 1. This means that the formal expansion is of the (m + 1)th order of accuracy.

3. Results and Discussion

For the convenience of writing and in order to be consistent with our references (such as Verhulst [5]), we consider the model

 $\ddot{x} + x = -2\epsilon\dot{x}$

suppose the initial conditions are x(0) = a and $\dot{x}(0) = 0$. The exact solution to this problem is

$$x(t) = ae^{\varepsilon t} \cos\left(\sqrt{1-\varepsilon^2} t\right) + \varepsilon \frac{a}{\sqrt{1-\varepsilon^2}} e^{-\varepsilon t} \sin\left(\sqrt{1-\varepsilon^2} t\right)$$

substituting

$$x(t) = x_0(t) + \varepsilon x_1(t) + \varepsilon^2 \dots$$

into the model, we obtain

$$\begin{split} \ddot{x}_0 + x_0 &= 0, \\ \ddot{x}_n + x_n &= -2 \dot{x}_{n-1}, \ n = 1,2, ... \end{split}$$

now we put

$$\begin{array}{ll} x_0(0)=a\,, & \dot{x}_0(0)=(0) \\ x_n(0)=0\,, & \dot{x}_n(0)=0, n=1,\!2,\ldots. \end{array}$$

we obtain

$$x_0(t) = a \cos t$$

 $x_1(t) = a \sin t - at \cos t$

therefore, our solution based on the formal expansion is

 $x(t) = a \cos t + a\varepsilon(\sin t - t \cos t) + \varepsilon^2 \dots$

that is, the first order formal solution is

 $y_1(t) = a \cos t$

the second order formal solution is

$$y_2(t) = a \cos t + a\varepsilon(\sin t - t \cos t)$$

Remark: We choose to consider this problem, because this problem has an exact solution. We intentionally use the exact solution to verify the validity of formal expansion solutions. If the

formal expansion solutions are valid for solving problems having exact solutions, then we shall be sure to use the formal expansion method to solve problems with the exact solutions are not known. Note that in practice, exact solutions are generally not known. Now for numerical experiments, we take a = 1 and vary the values of ε . To get clear illustrations, we take $\varepsilon = 0.5$, 0.05, 0.025 respectively.

3.1. Simulation for Case $\epsilon = 0.5$

For the first case, we take $\varepsilon = 0.5$. Figure 1 shows the exact solution, the first order formal expansion solution, and the second order formal expansion solution on the interval $0 \le t \le 1$. We observe that the second order solution approximates the exact solution better than the first order does in the domain $0 \le t \le 1$. However, if we extend the domain to be $0 \le t \le 10$, the second order solution behaves poorly and even worse than the first order solution, as given in Figure 2.

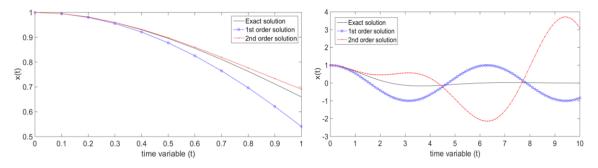


Figure 1. Exact, first order, and second order solutions for $\varepsilon = 0.5$ in domain $0 \le t \le 1$

Figure 2. Exact, first order, and second order solutions for $\varepsilon = 0.5$ in domain $0 \le t \le 10$

3.2. Simulation for Case $\epsilon = 0.05$

For the second case, we take $\varepsilon = 0.05$. Figure 3 shows the solutions on the interval $0 \le t \le 10$. Similar to the previous case, we observe that the second order solution approximates the exact solution better than the first order does in the domain $0 \le t \le 1$ and the extended domain $0 \le t \le 10$. However, if we extend the domain further to be $0 \le t \le 50$, the second order solution behaves worse than the first order solution, as illustrated in Figure 4.

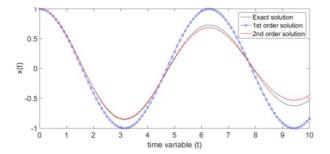


Figure 3. Exact, first order, and second order solutions for $\varepsilon = 0.05$ in domain $0 \le t \le 10$

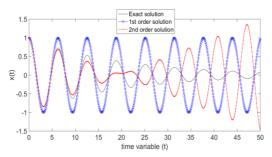
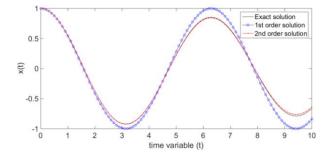


Figure 4. Exact, first order, and second order solutions for $\varepsilon = 0.05$ in domain $0 \le t \le 50$

3.3. Simulation for Case $\epsilon = 0.025$

As the third case, we fix $\varepsilon = 0.025$. We plot the solutions on the interval $0 \le t \le 10$ as shown in Figure 5. Once again, we observe that the second order solution approximates the exact solution better than the first order does in the domain $0 \le t \le 1$ and the extended domain $0 \le t \le 10$. However, once again, if we extend the domain further to be $0 \le t \le 100$, the second order solution behaves worse than the first order solution, as illustrated in Figure 6.

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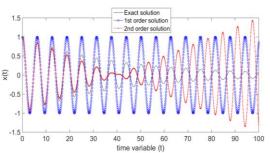


Figure 5. Exact, first order, and second order solutions for $\varepsilon = 0.025$ in domain $0 \le t \le 10$

Figure 6. Exact, first order, and second order solutions for $\varepsilon = 0.025$ in domain $0 \le t \le 100$

3.4. Simulation for the Validity of Order of Accuracy

As we have mentioned in the mathematical method section, the formal expansion is guaranteed to be valid only on the time-scale 1. For any extension of the domain larger than $0 \le t \le 1$, the accuracy is not guaranteed. Obviously from the previous subsections (Subsections 3.1-3.3), we obtain that for an extended domain, the errors of the formal expansion solutions are indeed very large. In the present subsection we investigate the validity of the order of accuracy of the formal expansion. We limit our domain only on the interval of the version of the time-scale 1. We take a discrete time domain to be t = 0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1. This means that we have discretised the time domain into 11 points. Error of an approximate solution is quantified as

$$Error = \frac{1}{N} \sum_{i=1}^{N} |x(t_i) - y(t_i)|$$

where *N* is the number of discrete time points t_i (in this case i = 1, 2, 3, ..., N with N = 11), x(t) is the exact solution, and y(t) is the approximate solution. Furthermore, the order of accuracy is calculated as:

$$Order of \ accuracy = \frac{log\left(\frac{Error_{j}}{Error_{j+1}}\right)}{log\left(\frac{\varepsilon_{j}}{\varepsilon_{j+1}}\right)}$$

the order of accuracy is calculated based on the *j*th and the (j + 1)th simulations, respectively, using different values of ε . Our results of errors and orders of accuracy are summarised in Tables 1 and 2. Table 1 contains the errors of the first order formal solution with respect to varying ε on the time-scale 1. As ε tends to zero, the order of accuracy approaches 1. This is consistent with the theoretical background that the solution is of the first order. Table 2 summarises the errors of the second order formal solution with respect to varying ε on the time-scale 1. We find that as ε tends to zero, the order of accuracy approaches 2. This is consistent with the theory that as it is the second order formal expansion solution, the order of accuracy is 2 in the time-scale 1.

Table 1. Errors of the First Order Formal	
Solution with Respect to Varving ε	

-			
on the Time-Scale 1			Scale 1
	Е	Error	Order of
			accuracy
	0.5	0.0351	-
	0.25	0.0193	0.86
	0.125	0.0101	0.93
	0.0625	0.0052	0.96
	0.03125	0.00	0.98

Table 2. Errors of the Second Order Formal
Solution with Respect to Varying ε

			, ,
on the Time-Scale 1			Scale 1
	ε	Error	Order of
			accuracy
	0.5	0.007527	-
	0.25	0.002037	1.89
	0.125	0.000531	1.94
	0.0625	0.000136	1.97
	0.03125	0.000034	1.98

As final remarks, knowing the accuracy of the formal expansion method, we could extend the application of this method to solve other mathematical engineering problems, such as those studied by researchers in [16-26]. Possible other problems to be solved using the formal expansion method could be those in [27-37].

4. Conclusion

We have provided our research results on the formal expansion method for solving an electrical circuit model. The accuracy of the formal expansion is guaranteed on the time-scale 1. We have also confirmed the order of accuracy for the first and second order formal expansion solution using numerical experiments. We obtain that for the first order formal expansion solution, as the perturbation factor is halved, the error is also halved on the time-scale 1. For the second order formal expansion solution, as the perturbation factor is halved, the error is quartered on the time-scale 1. With these results, the formal expansion method could be used to solve other problems in electrical circuits for the time-scale 1. When the time-scale is not equal to 1, we may need to do re-scaling so that the time domain is on the time-scale 1. This could be a future research direction.

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References

- [1] Sutikno T, Idris NRN, Widodo NS, Jidin A. FPGA Based a PWM Technique for Permanent Magnet AC Motor Drives. *International Journal of Reconfigurable and Embedded Systems.* 2012; 1(2): 43-48.
- [2] Sutikno T, Idris NRN, Jidin A, Jopri MH. FPGA Based Optimized Discontinuous SVPWM Algorithm for Three Phase VSI in AC Drives. *International Journal of Power Electronics and Drive System*. 2013; 3(2): 228-240.
- [3] Sutikno T, Idris NRN, Jidin AZ. Overview on Strategies and Approaches for FPGA Programming. *TELKOMNIKA Telecommunication Computing Electronics and Control.* 2014; 12(2): 273-282.
- [4] Sutikno T, Jidin AZ, Jidin A, Idris NRN. Strategies for FPGA Implementation of Non-Restoring Square Root Algorithm. *International Journal of Electrical and Computer Engineering*. 2014; 4(4): 548-556.
- [5] Verhulst F. Nonlinear Differential Equations and Dynamical Systems. Second, Revised and Expanded Edition. Berlin: Springer. 1996.
- [6] Zanette DH. Effects of Noise on the Internal Resonance of a Nonlinear Oscillator. *Scientific Reports.* 2018; 8: 5976.
- [7] Hellevik K, Gudmestad OT. *Limit Cycle Oscillations at Resonances*. IOP Conference Series: Materials Science and Engineering. 2017; 276: 012020.
- [8] Kiss G, Lessard JP. Rapidly and Slowly Oscillating Periodic Solutions of a Delayed van der Pol Oscillator. *Journal of Dynamics and Differential Equations*. 2017; 29(4): 1233-1257.
- [9] Hussin WNW, Harun FN, Mohd MH, Rahman MAA. Analytical Modelling Prediction by Using Wake Oscillator Model for Vortex-induced Vibrations. *Journal of Mechanical Engineering and Sciences*. 2017; 11(4): 3116-3128.
- [10] Herrera L, Montano O, Orlov Y. Hopf Bifurcation of Hybrid van der Pol Oscillators. *Nonlinear Analysis: Hybrid Systems.* 2017; 26: 225-238.
- [11] Cherevko AA, Bord EE, Khe AK, Panarin VA, Orlov KJ. The Analysis of Solutions Behaviour of van der Pol Duffing Equation Describing Local Brain Hemodynamics. *Journal of Physics: Conference Series*. 2017; 894(1): 012012.
- [12] He L, Yi L, Tang P. Numerical Scheme and Dynamic Analysis for Variable-order Fractional van der Pol Model of Nonlinear Economic Cycle. *Advances in Difference Equations.* 2016; 2016(1): 195.
- [13] Rachunkova I, Tomecek J. Antiperiodic Solutions to van der Pol Equations with State-dependent Impulses. *Electronic Journal of Differential Equations.* 2017; 2017: 247.
- [14] Siewe RT, Talla AF, Woafo P. Response of a Resonant Tunnelling Diode Optoelectronic Oscillator Coupled to a Non-linear Electrical Circuit. *IET Optoelectronics.* 2016; 10(6): 205-210.
- [15] Hoveijn I. Stability Pockets of a Periodically Forced Oscillator in a Model for Seasonality. Indagationes Mathematicae. 2016; 27(5): 1204-1218.
- [16] Mezghani F, Barchiesi D, Cherouat A, Grosges T, Borouchaki H. Comparison of 3D Adaptive Remeshing Strategies for Finite Element Simulations of Electromagnetic Heating of Gold Nanoparticles. Advances in Mathematical Physics. 2015; 2015.

- [17] Dymnikova I, Galaktionov E, Tropp E. Existence of Electrically Charged Structures with Regular Center in Nonlinear Electrodynamics Minimally Coupled to Gravity. *Advances in Mathematical Physics.* 2015; 2015.
- [18] Vafeas P. Dipolar Excitation of a Perfectly Electrically Conducting Spheroid in a Lossless Medium at the Low-Frequency Regime. *Advances in Mathematical Physics*. 2018; 2018.
- [19] Morán-López A, Córcoles J, Ruiz-Cruz JA, Montejo-Garai JR, Rebollar JM. Electromagnetic Scattering at the Waveguide Step between Equilateral Triangular Waveguides. Advances in Mathematical Physics. 2016; 2016.
- [20] Mungkasi S. Adaptive Finite Volume Method for the Shallow Water Equations on Triangular Grids. *Advances in Mathematical Physics*. 2016; 2016.
- [21] Gómez-Aguilar JF, Escalante-Martínez JE, Calderón-Ramón C, Morales-Mendoza LJ, Benavidez-Cruz M, Gonzalez-Lee M. Equivalent Circuits Applied in Electrochemical Impedance Spectroscopy and Fractional Derivatives with and without Singular Kernel. *Advances in Mathematical Physics*. 2016; 2016; 1-15.
- [22] Gómez-Aguilar JF, Rosales-García J, Escobar-Jiménez RF, López-López MG, Alvarado-Martínez VM, Olivares-Peregrino VH. On the Possibility of the Jerk Derivative in Electrical Circuits. Advances in Mathematical Physics. 2016; 2016; 1-8.
- [23] Dymnikova I, Galaktionov E. Basic Generic Properties of Regular Rotating Black Holes and Solitons. *Advances in Mathematical Physics.* 2017; 2017; 1-10.
- [24] Sun D, Bao W, Li X. Analytic Calculation of Transmission Field in Homogeneously Layered Mediums Excited by EMP. Advances in Mathematical Physics. 2017; 2017; 1-8.
- [25] Gao S, Chen S, Ji Z, Tian W, Chen J. DC Glow Discharge in Axial Magnetic Field at Low Pressures. Advances in Mathematical Physics. 2017; 2017; 1-8.
- [26] Tao B. Model Equations for Three-Dimensional Nonlinear Water Waves under Tangential Electric Field. Advances in Mathematical Physics. 2017; 2017; 1-8.
- [27] Supriyadi B, Mungkasi S. Finite Volume Numerical Solvers for Non-Linear Elasticity in Heterogeneous Media. *International Journal for Multiscale Computational Engineering.* 2016; 14(5): 479-488.
- [28] Suzuki Y, Takahashi M. Multiscale Seamless-Domain Method Based on Dependent Variable and Dependent-Variable Gradients. *International Journal for Multiscale Computational Engineering*. 2016; 14(6): 607-630.
- [29] Krowczynski M, Cecot W. A Fast Three-Level Upscaling for Short Fiber-Reinforced Composites. International Journal for Multiscale Computational Engineering. 2017; 15(1): 19-34.
- [30] Panda N, Butler T, Estep D, Graham L, Dawson C. A Stochastic Inverse Problem for Multiscale Models. International Journal for Multiscale Computational Engineering. 2017; 15(3): 265-283.
- [31] Rojek J, Nosewicz S, Chmielewski M. Micro-Macro Relationships from Discrete Element Simulations of Sintering. *International Journal for Multiscale Computational Engineering*. 2017; 15(4): 323-342.
- [32] Daniel YS, Aziz ZA, Ismail Z, Salah F. Entropy Analysis of Unsteady Magnetohydrodynamic Nanofluid over Stretching Sheet with Electric Field. *International Journal for Multiscale Computational Engineering*. 2017; 15(6): 545-565.
- [33] Sun W, Fish J, Dhia HB. A Variant of the S-Version of the Finite Element Method for Concurrent Multiscale Coupling. *International Journal for Multiscale Computational Engineering*. 2018; 16(2): 187-207.
- [34] Mungkasi S, Magdalena I, Pudjaprasetya SR, Wiryanto LH, Roberts SG. A Staggered Method for the Shallow Water Equations Involving Varying Channel Width and Topography. *International Journal for Multiscale Computational Engineering*. 2018; 16(3): 231-244.
- [35] Moyeda A, Fish J. Multiscale Analysis of Prestressed Concrete Structures. International Journal for Multiscale Computational Engineering. 2018; 16(3): 285-301.
- [36] Puszkarz AK, Krucinska I. Simulations of Air Permeability of Multilayer Textiles by the Computational Fluid Dynamics. *International Journal for Multiscale Computational Engineering*. 2018; 16(6): 509-526.
- [37] Li D, Fish J, Yuan ZF. Two-Scale and Three-Scale Computational Continua Models of Composite Curved Beams. International Journal for Multiscale Computational Engineering. 2018; 16(6): 527-554.