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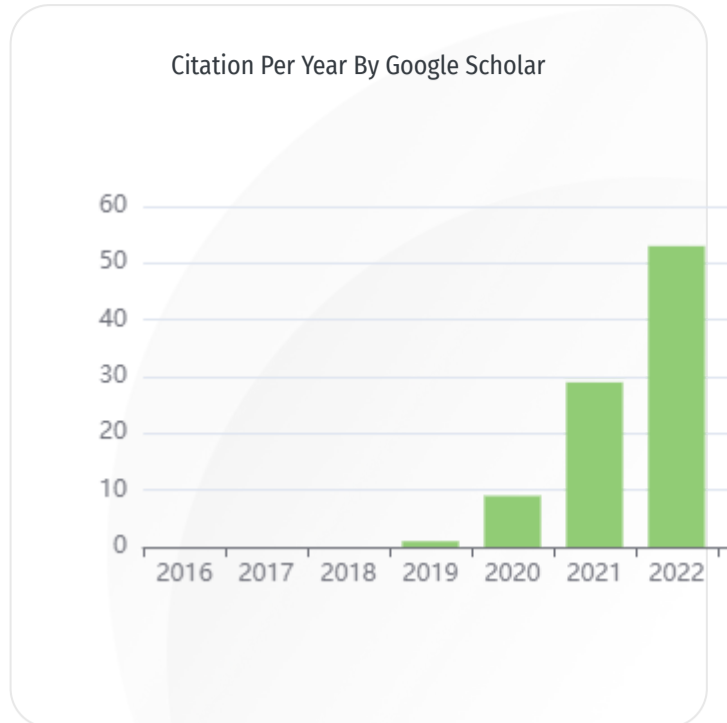
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# Design Of Maximum Torque Per Ampere Control Method In Squirrel Cage Three-Phase Induction Motor

Regina Chelinia Erianda Putri<sup>1,\*</sup>, Feri Yusivar<sup>2</sup>

<sup>1</sup>*Faculty of Science and Technology, Sanata Dharma University,  
Yogyakarta, 55281, Indonesia*

<sup>2</sup>*Faculty of Engineering, University of Indonesia, Depok, 16424, Indonesia*

\*Corresponding Author: [regina.chelinia@usd.ac.id](mailto:regina.chelinia@usd.ac.id)

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## Abstract

Improving the performance of three-phase induction motors is currently carried out by various control methods. One of them is controlling a three-phase induction motor using the Maximum Torque Per Ampere (MTPA) method. This paper focuses on the study of modeling specific motor models using the MTPA method. The purpose of the study is to prove that with the squirrel cage motor model, the speed can be increased above its rating. The MTPA method is a method of controlling a three-phase induction motor by controlling the current from the torque speed. Modeling is tested to see the responsiveness of the modeled system. The experimental results were tested using two-speed references and the system showed that MTPA control induction motors can improve the performance of three-phase induction motors. The results from the design show that the MTPA method can increase the performance of three-phase induction motors to reach 84.4%. The results of this study can be used as one way to model induction motors.

**Keywords:** Induction Motor, Modelling, MTPA

## 1 Introduction

Developments in the field of transportation in the current era are growing rapidly. However, it is not balanced with waste treatment, making the environment polluted with smoke pollution. According to the results of the study "In the last 100 years the earth has increased in temperature up to 0.18 degrees Celsius" [1].

The transition from fossil fuel energy to electrical energy as energy in the field of transportation requires one component of electric vehicle design, namely the induction

motor. A three-phase induction motor is an electronic device that aims to convert electrical energy into mechanical energy. A widely used induction motor is a three-phase induction motor known as an asynchronous motor, called because of the difference in speed from the rotation of the rotor to the rotation speed of the stator.

Such as previous research Direct Quadrature (D-Q) Modeling in the Speed Control System of Three Phase Induction Motors With Field Oriented Control (FOC) Based on P-I Controlled [2] about controlling induction motors with FOC based on PI controllers, and Speed Sensorless Control of Parallel Connected Dual Induction Motor Fed by Single Inverter using Direct Torque Control about controlling two induction motors with parallel induction motors [3]

The purpose of this study is to prove that with certain motorcycle models, speed can be increased above its rating. The MTPA method is a three-phase induction motor control method by adjusting the reference input of torque current and flux current to control the rotational speed of the induction motor. MTPA is designed to ensure that the current used is the minimum  $i_d$  current for development at motor torque, with the total stator flux controlled by the MTPA criterion.

## 2 Research Methodology

The system uses models and methods, namely induction motor models, Clark-Park transformation methods, Rotor Field Oriented Control (RFOC), and MTPA modeling.

### A. Induction motor model

Induction motor modeling uses the stator voltage vector  $(v_s)'$ , the stator current vector  $(i_s)'$ , the stator flux vector  $(\psi_s)'$  and the rotor flux vector  $(\psi_r)'$ . The general equation of induction motor is as follows

$$\vec{V}_s' = R_s \vec{i}_s' + \frac{d}{dt} \vec{\psi}_s' + j\omega_e \vec{\psi}_s' \quad (Eq. 1)$$

$$\vec{V}_r' = R_r \vec{i}_r' + \frac{d}{dt} \vec{\psi}_r' + j(\omega_e - \omega_r) \vec{\psi}_r' \quad (Eq. 2)$$

$$\vec{\psi}_s' = L_s \vec{i}_s' + L_m \vec{i}_r' \quad (Eq. 3)$$

$$\vec{\psi}_r' = L_r \vec{i}_r' + L_m \vec{i}_s' \quad (\text{Eq. 4})$$

### B. Clark-Park Transformation

The induction motor used is a three-phase induction motor, but modeling is carried out in two phases which aims to simplify calculations and analysis. Transformation from three phases to two phases, the transformations used are Clarke Transformation and Park Transformation.

The Clarke transform is a transformation that transforms a system that is on the ( $abc$  axis) into a stationary state frame of reference ( $\alpha\beta$  axis). In the stator frame of reference,  $\omega_e = 0$  and then in the cage rotor type, the terminals are briefly connected so that the rotor voltage is  $V_r = 0$ . The substitution of the equation of stator current and rotor current obtained induction motor model in the  $\alpha\beta$  axis becomes,

$$\frac{d}{dt} i_{s\alpha} = \left( -\frac{R_s}{\sigma L_s} - \frac{(1-\sigma)}{\sigma \tau_r} \right) i_{s\alpha} + \frac{L_m}{\sigma L_s L_r \tau_r} \psi_{r\alpha} + \frac{L_m \omega_r}{\sigma L_s L_r} \psi_{r\beta} + \frac{1}{\sigma L_s} V_{s\alpha} \quad (\text{Eq. 5})$$

$$\frac{d}{dt} i_{s\beta} = \left( -\frac{R_s}{\sigma L_s} - \frac{(1-\sigma)}{\sigma \tau_r} \right) i_{s\beta} - \frac{L_m \omega_r}{\sigma L_s L_r} \psi_{r\alpha} + \frac{L_m}{\sigma L_s L_r \tau_r} \psi_{r\beta} + \frac{1}{\sigma L_s} V_{s\beta} \quad (\text{Eq. 6})$$

$$\frac{d}{dt} \psi_{r\alpha} = \frac{R_r}{L_r} L_m i_{s\alpha} - \frac{R_r}{L_r} \psi_{r\alpha} - \omega_r \psi_{r\beta} \quad (\text{Eq. 7})$$

$$\frac{d}{dt} \psi_{r\beta} = \frac{R_r}{L_r} L_m i_{s\beta} + \omega_r \psi_{r\alpha} - \frac{R_r}{L_r} \psi_{r\beta} \quad (\text{Eq. 8})$$

with  $\sigma = \frac{L_s L_r - L_m^2}{L_s L_r}$  and  $\tau_r = \frac{L_r}{R_r}$

Park transform is a transformation that transforms a two-phase system that is on a stationary frame of reference ( $\alpha\beta$  axis) transformed in a rotating frame of reference ( $dq$  axis). In the rotor frame of reference the location  $\omega_e$  is put together by the axis of the rotor causing the magnitude of  $\omega_e$  is not equal to zero. The stator voltage transformation in equations (1)-(4) will be [4]:

$$\frac{d}{dt} i_{sd} = \left( -\frac{R_s}{\sigma L_s} - \frac{L_m^2}{\sigma L_s L_r \tau_r} \right) i_{sd} + \omega_e i_{sq} + \frac{L_m}{\sigma L_s L_r \tau_r} \psi_{rd} + \frac{L_m}{\sigma L_s L_r} \omega_r \psi_{rq} + \frac{1}{\sigma L_s} V_{sd} \quad (\text{Eq. 9})$$

$$\frac{d}{dt} i_{sq} = -\omega_e i_{sd} + \left( -\frac{R_s}{\sigma L_s} - \frac{L_m^2}{\sigma L_s L_r \tau_r} \right) i_{sq} - \frac{L_m}{\sigma L_s L_r} \omega_r \psi_{rd} + \frac{L_m}{\sigma L_s L_r \tau_r} \psi_{rq} + \frac{1}{\sigma L_s} V_{sq} \quad (\text{Eq. 10})$$

$$\frac{d}{dt} \psi_{rd} = \frac{R_r}{L_r} L_m i_{sd} - \frac{R_r}{L_r} \psi_{rd} + (\omega_e - \omega_r) \psi_{rq} \quad (\text{Eq. 11})$$



$$\frac{d}{dt} \psi_{rq} = \frac{R_r}{L_r} L_m i_{sq} - (\omega_e - \omega_r) \psi_{rd} - \frac{R_r}{L_r} \psi_{rq} \quad (Eq. 12)$$

with,  $\sigma = \frac{L_s L_r - L_m^2}{L_s L_r}$  and  $\tau_r = \frac{L_r}{R_r}$  and rotor speed equation  $\frac{d}{dt} \omega_r = \frac{T_e - T_l}{J}$ :

While the mechanical equation of a motor that has a polar p-tide. In this case, electromagnetic torque  $T_e$  expressed by,

$$T_e = p \left( \frac{L_m}{L_r} \right) (i_{s\beta} \psi_{r\alpha} - i_{s\alpha} \psi_{r\beta}) \quad (Eq.13)$$

$$T_e = p \left( \frac{L_m}{L_r} \right) (i_{sq} \psi_{rd} - i_{sd} \psi_{rq}) \quad (Eq. 14)$$

The parameters used are as follows:

$R_r$ = Resistance on the rotor ( $\Omega$ )	$V_{s\alpha}$ = Stator voltage on $\alpha$ axis (V)
$R_s$ = Resistance on the stator ( $\Omega$ )	$V_{s\beta}$ = Stator voltage on the $\beta$ axis (V)
$L_m$ = Magnetic inductance (H)	$V_{sd}$ = Stator voltage on the d-axis (V)
$L_s$ = Magnetic inductance (H)	$V_{sq}$ = Stator voltage on the q-axis (V)
$L_r$ = Magnetic inductance (H)	$\psi_{r\alpha}$ = Flux of $\alpha$ -axis rotor (Wb)
$\sigma$ = Leakage Coefficient	$\psi_{r\beta}$ = Flux of $\beta$ -axis rotor (Wb)
$i_{s\alpha}$ = $\alpha$ axis stator current (A)	$\psi_{rd}$ = d-axis rotor flux (Wb)
$i_{s\beta}$ = $\beta$ axis stator current (A)	$\psi_{rq}$ = q-axis rotor flux (Wb)
$i_{sd}$ = d-axis stator current (A)	$\omega_r$ = Rotor velocity (rad/s)
$i_{sq}$ = stator current q axis (A)	$\omega_e$ = Rotating field speed (rad/s)
$T_e$ = Electromagnetic torque (Nm)	$p$ = number of poles or poles
$T_l$ = Load torque (Nm)	$\tau_r$ = Rotor constant time

### C. Rotor Field Oriented Control (RFOC)

The orientation of the FOC (Field Oriented Control) control used has three frames of reference, named the rotor-stator and the air gap. RFOC not require additional processes to separate the interrelationships of variables in the equation. Rotor-oriented FOC (RFOC) can separate (declutch) flux and torque components so that they can be controlled by d-axis stator current ( $i_{sd}$ ) and q-axis stator current ( $i_{sq}$ ) respectively. The separation of the two components  $U_{sd}$  and  $U_{sq}$  is a linear part of the stator voltage after

the decoupling process.  $V_{cd}$  and  $V_{cq}$  are the non-linear part of the stator voltage after the decoupling process is carried out, as follows

$$U_{sd} = R_s i_{sd} + L_s \sigma \frac{d}{dt} i_{sd} \quad (\text{Eq. 15})$$

$$U_{sq} = R_s i_{sq} + L_s \sigma \frac{d}{dt} i_{sq} \quad (\text{Eq. 16})$$

$$V_{cd} = -\sigma L_s \omega_e i_{sq} + \frac{L_m}{L_r} \frac{d}{dt} \psi_{rd} \quad (\text{Eq. 17})$$

$$V_{cq} = \sigma L_s \omega_e i_{sd} + \frac{L_m}{L_r} \omega_e \psi_{rd} \quad (\text{Eq. 18})$$

Then the current controller model is modeled as follows:

$$v_{sd}^* = -k_{idp} i_{sd} + k_{idp} i_{sd}^* + k_{idi} x_{sd} - \sigma L_s N \omega_m i_{sq1}^* - \sigma L_s \frac{R_r}{L_r} \frac{i_{sq1}^{*2}}{i_{sd2}^*} \quad (\text{Eq. 19})$$

$$v_{sq}^* = -k_{iqp} i_{sq} + k_{iqp} i_{sq}^* + k_{iqi} x_{sq} + \sigma L_s N \omega_m i_{sd1}^* + \sigma L_s \frac{R_r}{L_r} \frac{i_{sd1}^* i_{sq1}^{*2}}{i_{sd2}^*} + (1 - \sigma) L_s N \omega_m i_{sd2}^* + \frac{(1 - \sigma) L_s R_r}{L_r} i_{sq1}^* \quad (\text{Eq. 20})$$

$$\text{Where } k_{idp} = \frac{\sigma L_s}{T_d}, k_{idi} = \frac{R_s}{T_d}, k_{iqp} = \frac{\sigma L_s}{T_d}, k_{iqi} = \frac{R_s}{T_d}$$

Further, the first order of the reference current of the slip frequency and decoupling calculation becomes,

$$\frac{d}{dt} i_{sd1}^* = \frac{1}{T_d} i_{sd}^* - \frac{1}{T_d} i_{sd1}^* \quad (\text{Eq. 21})$$

$$\frac{d}{dt} i_{sq1}^* = \frac{1}{T_d} i_{sq}^* - \frac{1}{T_d} i_{sq1}^* \quad (\text{Eq. 22})$$

$$\frac{d}{dt} i_{sd2}^* = \frac{1}{T_2} i_{sd}^* - \frac{1}{T_2} i_{sd2}^* \quad (\text{Eq.23})$$

#### D. MTPA Modelling

The process of the Maximum Torque Per Ampere Method in the MTPA condition process identified for a particular motor torque, the stator current components used are  $i_d$  and  $i_q$ . MTPA is operated under the condition of each  $d$  and  $q$  axis flux component in a synchronous reference frame using equations [5]. The Maximum Torque Per Ampere method is shown in Fig 1.

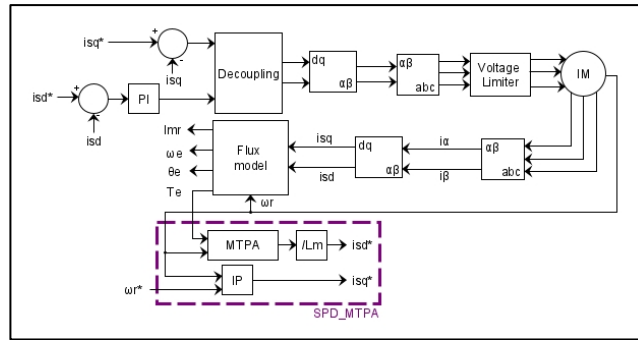


Figure 1. Block Process Diagram MTPA Method

The component values of the  $d$  and  $q$  axes for the flux synchronous reference frame for the MTPA method are given by the equation.

$$\psi_{ds}|_{TMPA} = \frac{L_s}{L_m} \sqrt{\frac{2T_e L_r}{P}} \quad (Eq. 24)$$

$$\psi_{qs}|_{TMPA} = \frac{\sigma L_s}{L_m} \sqrt{\frac{2T_e L_r}{P}} \quad (Eq. 25)$$

The values of the total flux components on the  $d$  and  $q$  axes in the synchronous reference frame are shown as

$$|\vec{\psi}_s|_{TMPA} = \frac{L_s}{L_m} \sqrt{\frac{2L_r(1+\sigma^2)T_e}{P}} \quad (Eq. 26)$$

Then substitute  $\omega_{sl} = \frac{R_r i_{sq1}^*}{L_r i_{sd2}^*}$ ,  $v_{sd} = v_{sd}^*$ , and  $v_{sq} = v_{sq}^*$ ,  $|\psi_s| = \frac{L_s}{L_m} \sqrt{\frac{2L_r(1+\sigma^2)i_{sq}^*}{P}}$  so

$$i_{sd}^* = 1 + \frac{L_s}{L_m^2} \sqrt{\frac{2L_r(1+\sigma^2)i_{sq}^*}{P}}$$

The modeling results that have been linearized into,

$$\begin{aligned} \frac{d}{dt} \Delta i_{sd} = & \left( -\frac{k_{idp} + R_s}{\sigma L_s} - \frac{R_r(1-\sigma)}{\sigma L_r} \right) \Delta i_{sd} + \left( N\omega_{m0} + \frac{R_r i_{sq10}^*}{L_r i_{sd20}^*} \right) \Delta i_{sq} + \left( \frac{L_m R_r}{\sigma L_s L_r^2} \right) \Delta \psi_{rd} + \left( \frac{N L_m \omega_{m0}}{\sigma L_s L_r} \right) \Delta \psi_{rq} + \\ & \left( \frac{k_{idi}}{\sigma L_s} \right) \Delta x_{sd} + \left( \frac{R_r i_{sq0}^*}{L_r i_{sd20}^*} - \frac{2R_r i_{sq10}^*}{L_r i_{sd20}^*} - N\omega_{m0} \right) \Delta i_{sq1} + \left( -\frac{R_r i_{sq0}^* i_{sq10}^*}{L_r i_{sd20}^*} + \frac{R_r i_{sq10}^*{}^2}{L_r i_{sd20}^*} \right) \Delta i_{sd2} + \\ & \left( \frac{1}{2} \frac{k_{idp}}{\sigma L_m^2} \left( \frac{2L_r(1+\sigma^2)i_{sq0}^*}{P} \right)^{\frac{1}{2}} \right) \Delta i_{sq} + \left( N i_{sq0} + \frac{N L_m \psi_{rq0}}{\sigma L_s L_r} - N i_{sq10} \right) \Delta \omega_m \quad (Eq. 27) \end{aligned}$$

$$\begin{aligned} \frac{d}{dt} \Delta i_{sq} = & \left( -N\omega_{m0} - \frac{R_r i_{sq10}^*}{L_r i_{sd20}^*} \right) \Delta i_{sd} + \left( -\frac{k_{iqp} + R_s}{\sigma L_s} - \frac{R_r(1-\sigma)}{\sigma L_r} \right) \Delta i_{sq} + \left( -\frac{N L_m \omega_{m0}}{\sigma L_s L_r} \right) \Delta \psi_{rd} + \left( \frac{L_m R_r}{\sigma L_s L_r^2} \right) \Delta \psi_{rq} + \\ & \left( \frac{k_{iqi}}{\sigma L_s} \right) \Delta x_{sq} + \left( N\omega_{m0} + \frac{R_r i_{sq10}^*}{L_r i_{sd20}^*} \right) \Delta i_{sd1} + \left( -\frac{R_r i_{sd0}^*}{L_r i_{sd20}^*} + \frac{(1-\sigma)R_r}{\sigma L_r} + \frac{R_r i_{sd10}^*}{L_r i_{sd20}^*} \right) \Delta i_{sq1} + \end{aligned}$$

$$\left( \frac{R_r i_{sd0} i_{sq10}^*}{L_r i_{sd20}^2} - \frac{R_r i_{sd10}^* i_{sq10}^*}{L_r i_{sd20}^2} + \left( \frac{(1-\sigma)N\omega_{m0}}{\sigma} \right) \right) \Delta i_{sd2}^* + \left( \frac{k_{iqp}}{\sigma L_s} \right) \Delta i_{sq}^* + \left( -N i_{sd0} + N i_{sd0}^* - \frac{NL_m \psi_{rd0}}{\sigma L_s L_r} + \frac{(1-\sigma)N i_{sd20}^*}{\sigma} \right) \Delta \omega_m \quad (Eq. 28)$$

$$\frac{d}{dt} \Delta \psi_{rd} = \left( \frac{L_m R_r}{L_r} \right) \Delta i_{sd} + \left( -\frac{R_r}{L_r} \right) \Delta \psi_{rd} + \left( \frac{R_r i_{sq10}^*}{L_r i_{sd20}^*} \right) \Delta \psi_{rq} + \left( \frac{R_r \psi_{rq0}}{L_r i_{sd20}^*} \right) \Delta i_{sq1} + \left( -\frac{R_r i_{sq10}^* \psi_{rd0}}{L_r i_{sd20}^2} \right) \Delta i_{sd2}^* \quad (Eq. 29)$$

$$\frac{d}{dt} \Delta \psi_{rq} = \left( \frac{L_m R_r}{L_r} \right) \Delta i_{sq} + \left( \frac{R_r i_{sq10}^*}{L_r i_{sd20}^*} \right) \Delta \psi_{rd} + \left( -\frac{R_r}{L_r} \right) \Delta \psi_{rq} + \left( -\frac{R_r \psi_{rd0}}{L_r i_{sd20}^*} \right) \Delta i_{sq1} + \left( \frac{R_r i_{sq10}^* \psi_{rd0}}{L_r i_{sd20}^2} \right) \Delta i_{sd2}^* \quad (Eq. 30)$$

$$\frac{d}{dt} \Delta \omega_m = \left( -\frac{NL_m \psi_{rq0}}{J L_r} \right) \Delta i_{sd} + \left( \frac{NL_m \psi_{rd0}}{J L_r} \right) \Delta i_{sq} + \left( \frac{NL_m i_{sq0}^*}{J L_r} \right) \Delta \psi_{rd} + \left( -\frac{NL_m i_{sd0}^*}{J L_r} \right) \Delta \psi_{rq} + \left( -\frac{1}{J} \right) \Delta T_L \quad (Eq. 31)$$

$$\frac{d}{dt} \Delta x_{sd} = [-1] \Delta i_{sd} + \left( \frac{1}{2} \frac{L_s}{L_m^2} \left( \frac{2L_r(1+\sigma^2) i_{sq0}^*}{P} \right)^{-\frac{1}{2}} \right) \Delta i_{sq}^* \quad (Eq. 32)$$

$$\frac{d}{dt} \Delta x_{sq} = [-1] \Delta i_{sq} + [1] \Delta i_{sq}^* \quad (Eq. 33)$$

$$\frac{d}{dt} \Delta i_{sd1}^* = \left[ -\frac{1}{T_d} \right] \Delta i_{sd1}^* + \left[ \frac{1}{T_d} \right] \left( \frac{1}{2} \frac{L_s}{L_m^2} \left( \frac{2L_r(1+\sigma^2) i_{sq0}^*}{P} \right)^{-\frac{1}{2}} \right) \Delta i_{sq}^* \quad (Eq. 34)$$

$$\frac{d}{dt} \Delta i_{sq1}^* = \left[ -\frac{1}{T_d} \right] \Delta i_{sq1}^* + \left[ \frac{1}{T_d} \right] \Delta i_{sq}^* \quad (Eq. 35)$$

$$\frac{d}{dt} \Delta i_{sd2}^* = \left[ -\frac{1}{T_2} \right] \Delta i_{sd2}^* + \left[ \frac{1}{T_2} \right] \left( \frac{1}{2} \frac{L_s}{L_m^2} \left( \frac{2L_r(1+\sigma^2) i_{sq0}^*}{P} \right)^{-\frac{1}{2}} \right) \Delta i_{sq}^* \quad (Eq. 36)$$

With the equilibrium point as shown by  $\omega_{m0} = 209.4254$ ,  $i_{sd0}^* = 1$ ,  $i_{sq0}^* = 0.23914$

### 3 Results and Discussions

The induction motor used in this modeling uses an induction motor with specifications, namely a three-phase induction motor, 750 W, 1410 rpm, and 4 poles.

**Table 1.** Parameters of Induction Motor

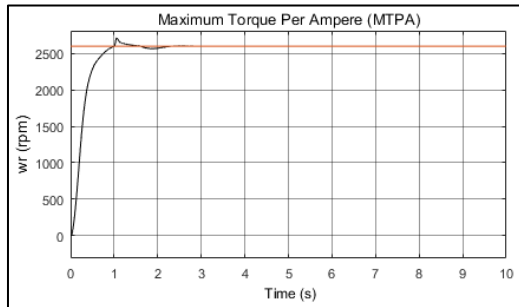
Parameter	Symbol	Value
Pole pairs	P	2
Stator Resistance	$R_s$	2.76 $\Omega$
Rotor Resistance	$R_r$	2.9 $\Omega$
Stator Inductance	$L_s$	0.2349 H
Rotor Inductance	$L_r$	0.2349 H
Mutual Inductance	$L_m$	0.2279 H

The controller parameters used in the simulation process of each method are shown in Table 1-2.

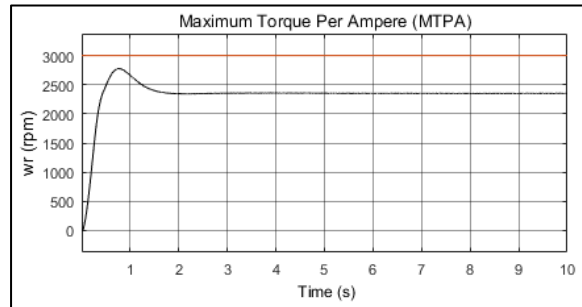
**Table 2.** Controller Parameters

Parameter	Symbol	Value
Kp Speed Controller	Kp	0.9
Ki Speed Controller	Ki	0.2

Modeling test by providing several reference speed inputs at 2600 rpm and 3000 rpm.



**Figure 2.** MTPA at 2600 rpm



**Figure 3.** MTPA at 3000 rpm

a. Testing with 2600 rpm speed reference

The test was carried out by providing a reference of 2600 rpm. The response of the system is shown in Fig 2. The response of the system can follow its reference speed, in simulations, there are overshoots and several oscillations, and the time required to reach a steady state. However, the system can reach a steady-state state.

b. Testing with reference speed 3000 rpm.

The test was carried out by providing a reference of 3000 rpm. The response of the system is shown in Fig 3. The response of the system cannot follow the reference speed, because the desired speed has exceeded the speed limit of the system. The system will only stay in the steady-state position even if it not reach its target speed.

## 4 Conclusions

Studies on modeling with the Maximum Torque Per Ampere (MTPA) Method have been presented. The result of the modeling is that increasing the speed of each different reference input will affect settling time. The higher the speed, the longer it takes for the system to reach a steady-state state. The maximum speed that can be achieved is at a speed of 2600 rpm, so the MTPA method can increase the performance of three-phase induction motors by 84.4%. The above research is limited to the induction motor used is

a squirrel cage type three-phase induction motor, and the system uses a speed sensor. The next research direction is to prove the stability of the system by analyzing pole position and movement with variations of  $K_p$ ,  $K_i$ , and  $K_d$  and combining the MTPA method with other methods to improve the performance of the induction motor.

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